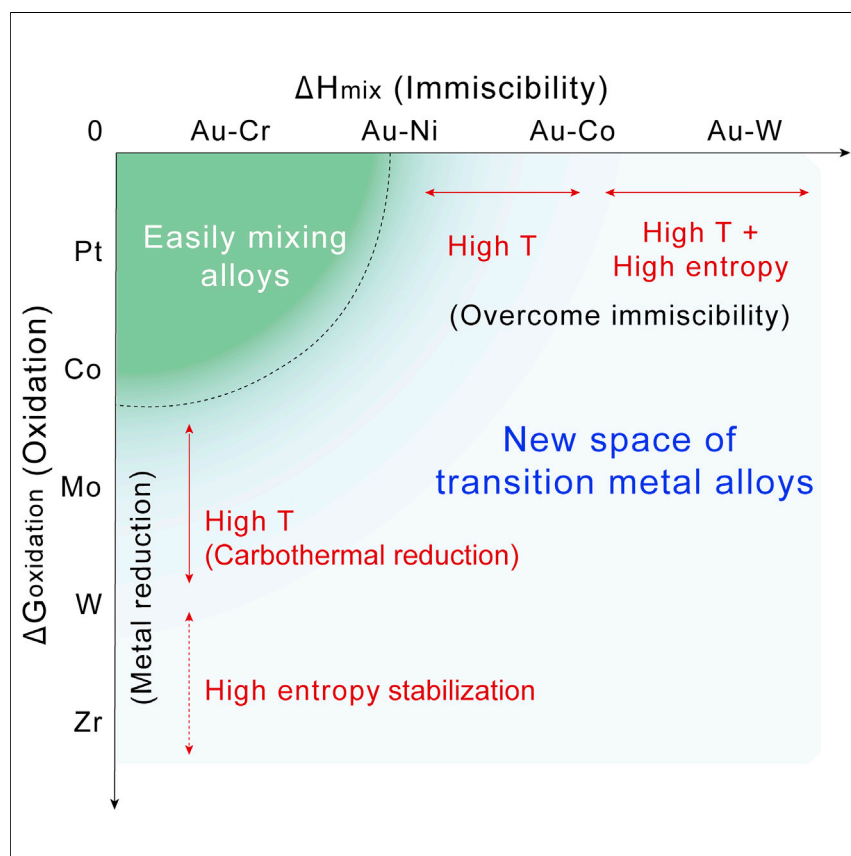


Article

Extreme mixing in nanoscale transition metal alloys



Conventionally, alloys are mostly synthesized in the region of easy mixing, i.e., with light immiscibility and oxidation potentials. Yet such a limited elemental combination largely hinders possible tunability and material discovery. By using entropic design (high temperature and high entropy) that favors uniform mixing, we extended nanoscale alloying to previous unmixable regions by including strongly immiscible and easily oxidized combinations, which we called an extreme mixing. The new alloy space could bring forth exotic nanomaterials for broad applications.

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Highlights

A record 15-element nanoalloy was achieved by extreme entropic design and stabilization

Nanoscale alloys entered into regions featuring strong immiscibility and easy oxidation

Mixing enthalpy and Ellingham diagram can effectively guide the nanoscale alloy design

The first observation of localized strain and lattice distortions in extreme nanoalloys



Benchmark

First qualification/assessment of material properties and/or performance

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Article

Extreme mixing in nanoscale transition metal alloys

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SUMMARY

The ability to alloy different elements is critical for property tuning and materials discovery. However, general alloying at the nanoscale remains extremely challenging due to strong immiscibility and easy oxidation, particularly for early transition metals that are highly reactive. Here, we report nanoscale alloying using a high-temperature- and high-entropy-based strategy ($T^*\Delta S_{\text{mix}}$) to significantly expand the possible alloys and include early transition metals. While high-temperature synthesis favors alloy formation and metal reduction, the high-entropy compositional design is critical to further extending the alloying to strongly repelling combinations (e.g., Au-W) and easily oxidized elements (e.g., Zr). In particular, we explicitly characterized a record 15-element nanoalloy, which showed a solid-solution structure featuring localized strain and lattice distortions as a result of extreme mixing. Our study significantly broadens available compositions of nanoalloys and provides clear guidelines by utilizing the less-explored entropic chemistry.

INTRODUCTION

Alloys represent a vast compositional space for material discovery. In particular, transition metal alloys offer largely tunable performances through strong interactions and hybridization of multielement chemistry, which can lead to superior reactivity and selectivity in a range of thermo- and electrocatalysis applications.^{1–6} However, considering the wide range of transition metals from group IV to group XI, alloying these largely different elements has proved extremely challenging.^{5,7,8} Figure 1A shows the physicochemical differences among transition metals with a wide range of atom sizes, valences, electronegativity, and crystalline structures (see also Table S1), which would lead to immiscibility and failure of alloying. In addition, non-noble transition elements are easily oxidized, particularly for early transition metals that are highly reactive and oxophilic,^{1,9} resulting in oxide phases and failure of metallic alloying. For instance, W strongly repels Au, while Zr has a highly negative oxidation potential, and no alloy was reported at nanoscale among these combinations. As previous literature shows, out of the vast potential compositional space for five component systems (e.g., $>10^5$ equal molar compositions), only a few hundred (~ 200) are single phases as predicted by theoretical calculations,^{10–12} demonstrating the scarcity and challenge of uniform alloying.

Traditionally, the Hume-Rothery alloying rule¹³ guides bulk alloy formation by limiting the compositions to only similar elements (i.e., atomic size difference [δ]

Progress and potential

New materials with exotic functionalities are most often constructed by alloying. However, such a capability is constrained by elemental or phase immiscibility, which are even exaggerated at nanoscale due to the short diffusion length and easy oxidation. Hume-Rothery rules could guide the alloy design and formation but are largely limited to narrow combinations and bulk scale scenarios. In this work, we proposed the use of extreme entropic driving force—high-temperature ($\sim 1,800$ K) and high-entropy (15 element) design—to largely extend such an alloy space at nanoscale to include strongly immiscible and easily oxidized combinations. In addition, the mixing enthalpy and Ellingham diagram provide critical guidelines for nanoscale alloy design and prediction. As a result of extreme mixing, we observed localized strain and lattice distortions in these entropy-stabilized nanoalloys. This study opens up a vast space for nanoscale material manipulation and discovery.

of <15%, similar structure, valences, and electronegativity). Quantitatively, density functional theory has predicted ~ 900 binary metallic combinations and has found a small mixing enthalpy $\Delta H_{\text{mix}} < 37$ meV (3.57 kJ/mol) that is a safe upper limit for uniform alloying by data analysis among numerous experimental reports.¹⁰ Similar empirical single-phase selection rules have been established in multielement high-entropy alloys (HEAs), again by restricting the possible alloy elements to a range of approximately $-15 \text{ kJ/mol} < \Delta H_{\text{mix}} < 5 \text{ kJ/mol}$ and $0 < \delta < 5\%$, or similar confinement.^{10–12,14–18} As a result, facile alloying is generally found under restricted conditions for elements with a small mixing enthalpy and oxidation potential, as shown in the range within the green line in Figure 1B. Nevertheless, these existing phase selection rules render very limited alloys and largely restricted compositional spaces for material discovery. Moreover, the extremely small short diffusion length for nanoscale particles accelerates potential phase separation, oxidation, and therefore failure of alloying.^{7,8,19,20} Consequently, literature reports on extreme mixing (i.e., mixing of previously unmixable elements) for nanoscale alloys beyond existing rules are rare, and there are no clear guidelines on nanoalloy design and synthesis.

Here, we report the systematic study of alloying in an extended spectrum of transition metals with a focus on addressing the immiscibility and oxidation problems that occur in nanoscale alloying. In contrast to the existing rules that restrict alloys among only similar elements, we used a high-temperature- and high-entropy-based strategy ($T^*\Delta S_{\text{mix}}$) to drive alloy formation thermodynamically, which is non-specific to alloy compositions and thus enables general alloying (Figure 1B). In addition, the high-temperature synthesis can induce nanoscale metal reduction and avoid oxide impurities. Kinetically, the high-entropy structure features multielement mixing with distorted lattices, which could stabilize those immiscible combinations and reduced elements into entropy-stabilized alloys, featuring extreme mixing alloys that were not previously possible. Here, we denote “extreme mixing” as alloy formation beyond the prediction by existing rules.

As shown in Figure 1C, our study increased the synthesis temperature from regular nanomaterial synthesis at 300–800 K to a high temperature of 1,800 K and the configurational entropy from binary ($\Delta S_{\text{conf}} = 5.76 \text{ J/mol/K}$) to 15-element mixing ($\Delta S_{\text{conf}} = 22.51 \text{ J/mol/K}$), thereby substantially increasing the entropic contribution $T^*\Delta S_{\text{mix}}$ by ~ 8 -fold to $\sim 40 \text{ kJ/mol}$, which is critical in counterbalancing the enthalpy penalty and driving alloy formation ($\Delta G_{\text{mix}} = \Delta H_{\text{mix}} - T^*\Delta S_{\text{mix}}$). Based on our synthesis, we demonstrated an extreme mixing of 15 early and late transition metals in a uniform alloy structure, including strongly repelling Au and W, as shown in the element mapping by scanning transmission electron microscopy (STEM) (Figure 1D). Note that Sn is included because it is intensively studied for alloying with transition metals for catalysis and energy applications.^{21–23} Therefore, by using the entropic contribution, our study significantly extends the mixing potential of transition metals and acts as a guideline for nanoscale alloy synthesis.

RESULTS

Entropic contribution to overcoming immiscibility

Au-based binary systems with a wide range of mixing enthalpy (calculated by density functional theory,¹⁰ Table S2) were chosen to explore the synthetic boundaries of entropic driving force to overcome immiscibility. For example, Au-Ni has a mixing enthalpy $\Delta H_{\text{mix}} = 4.25 \text{ kJ/mol}$, which is beyond the single-phase alloy rules and shows a large immiscible gap in the phase diagram at low temperature (Figure 2A). This is confirmed by wet chemical synthesis of Au-Ni (and Au-Co) showing clear

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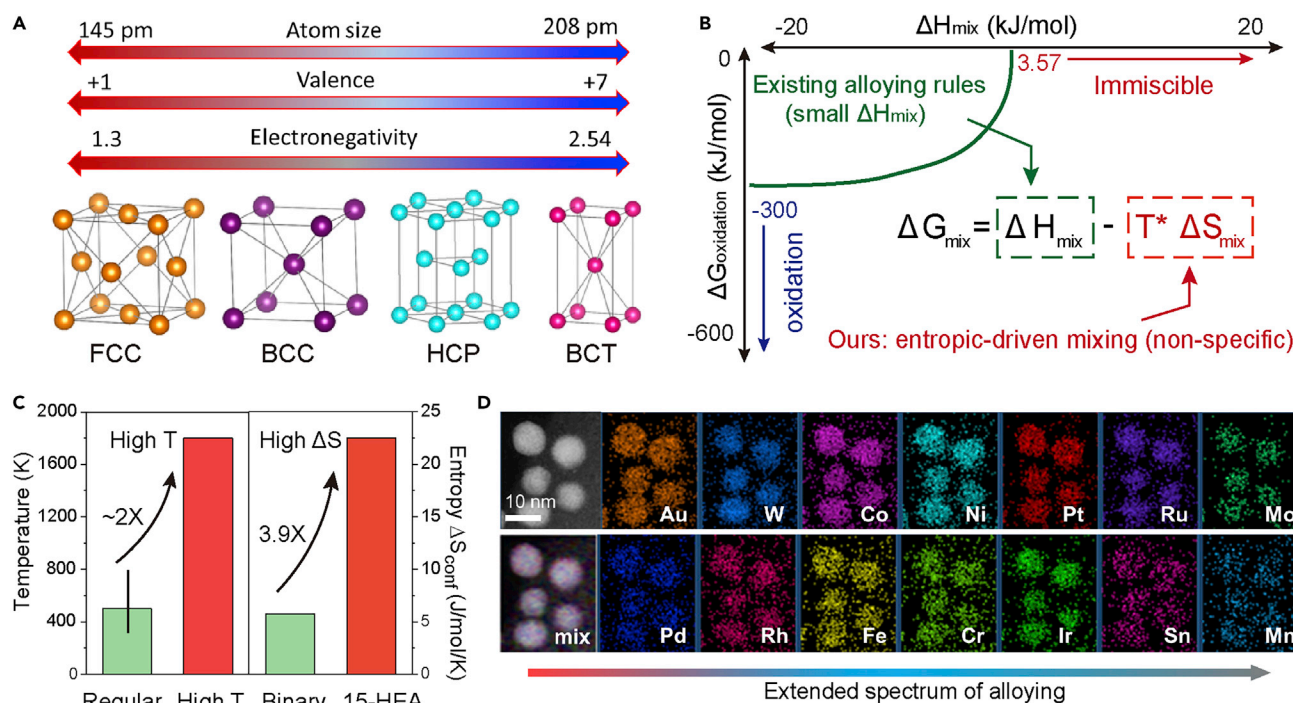


Figure 1. Extreme alloying by a high-temperature and high-entropy synthesis

(A) Transition metal elements and their largely different physiochemical properties.

(B) Existing single-phase alloying rule (a small ΔH_{mix}) and our strategies based on the entropic contribution ($-T\Delta S_{\text{mix}}$) to enable more alloy choices.

(C) The high temperature and high entropy (configurational entropy) in this study (1,800 K, 15 element mixing) compared with typical nanomaterial studies (300–800 K, binary systems), rendering an entropic driving force of approximately -40 kJ/mol.

(D) STEM elemental maps of extreme mixing in nanoparticles containing 15 different elements including both late and early transition metals, made possible by the high-temperature and high-entropy synthesis (Cu mapping data is not shown due to use of the Cu grid).

phase separation toward hybrid nanoparticles.²⁴ However, at high temperatures, Au-Ni can be uniformly mixed owing to the increasing temperature and entropy that drive the alloy formation. Therefore, a rapid high-temperature synthesis could lead to uniform alloy formation whereby the high temperature drives the alloy mixing while the subsequent rapid cooling can help maintain the small size distribution and uniform alloy structure.^{18,25–31}

Experimentally, we synthesized AuNi binary alloy nanoparticles on a carbon nanofiber substrate using carbothermal shock synthesis⁵ driven by direct Joule heating (e.g., 1,800 K, 50 ms; see [experimental procedures](#) and [Figure S1](#)). The process is similar to previous non-equilibrium synthesis,^{5,32} but this work focuses on discovering and exploring alloying principles and guidelines in transition metal alloys using the less-explored entropic term. In particular, the kinetic quenching (cooling rate on the order of 10^4 – 10^5 K/s) maximized the possibility of alloy formation by eliminating the possible phase separation during slow cooling. After synthesis, we observed uniform nanoparticles dispersed on the carbon substrate ([Figure S2A](#)) and confirmed a face-centered-cubic (FCC) single-phase alloy structure by X-ray diffraction (XRD) ([Figure 2B](#)). In comparison, a low-temperature control synthesis (~ 800 K, 50 ms, repeated three times for a complete reaction) leads to a clear peak splitting in XRD, indicating the importance of high-temperature synthesis ([Figure 2B](#)). Using the same high-temperature process, we also synthesized Au-based alloys previously considered immiscible with a range of mixing enthalpy,^{10,24} including AuNi, AuFe, and AuCo, which now demonstrate a single-phase structure confirmed by powder

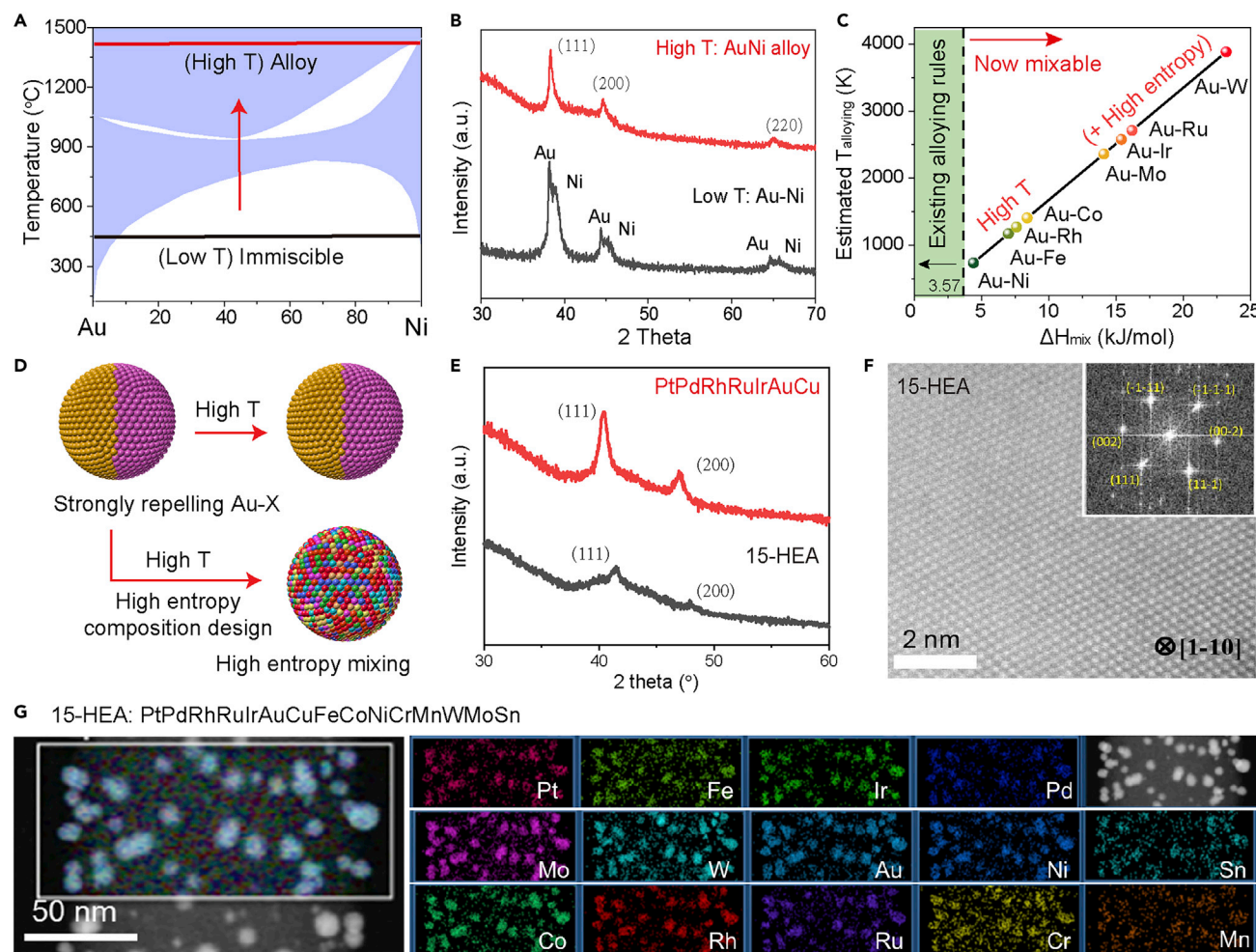


Figure 2. Overcoming immiscibility by high-temperature and high-entropy synthesis

(A) Phase diagram of Au-Ni, showing the immiscible region at low temperature.

(B) XRD profiles of Au-Ni synthesized by high-temperature shock (1,800 K, a single-phase structure) and low-temperature shock (800 K, phase separation of Au and Ni).

(C) Summary of general alloying in Au-based binary combinations. The high-temperature synthesis extends the alloying of elements up to Au-Co, while further extension requires a high-entropy compositional design. The alloying temperature is estimated from $T_{\text{alloying}} = \Delta H_{\text{mix}} / \Delta S_{\text{mix}}$.

(D) Schematic demonstrating the mixing of strongly repelling Au-X combinations with a high-entropy design.

(E) XRD profiles of a 7-element system of noble transition metals and a 15-HEA formulation; both samples show a single-phase structure despite containing strongly repelling combinations.

(F) Atomic-resolution HAADF image of a 15-HEA nanoparticle showing an FCC pattern (inset).

(G) Low-magnification element maps for 15-HEA nanoparticles, showing uniform mixing of early and late transition metals.

See also [Figures S1–S4](#).

XRD as well as transmission electron microscopy (TEM) energy-dispersive X-ray spectroscopy (EDS) mapping ([Figures 2B](#) and [S2](#)). However, for combinations that are strongly repelling, like Au-Ru and Au-W ($\Delta H_{\text{mix}} > 10$ kJ/mol), we still observe phase separation in these binary compositions despite using high-temperature synthesis ([Figure S2B](#)).

We hypothesized that increasing the mixing entropy could further increase the entropic contribution in free energy to counterbalance the large mixing enthalpy, which should enable alloy formation in systems that are strongly repelling ([Figure 2D](#)). As an example, we applied high-temperature shock to a 7-element system

of noble metals (PtPdRuRhIrAuCu) and observed single-phase mixing as revealed by the XRD profile (Figure 2E), indicating alloying of repelling Au-Ir and Au-Ru. By further increasing the mixing entropy, we synthesized a high-entropy alloy system composed of PtPdRhRuIrAuCuFeCoNiCrMnWMoSn (denoted 15-HEA nanoalloy) uniformly dispersed on the carbon substrates (TEM images in Figure S3). This alloy contains many immiscible combinations and still shows a single-phase structure (Figure 2E), although the diffraction peaks are broadened due to the lattice mismatch among these 15 elements. A high-resolution high-angle annular dark-field scanning electron microscopy (HAADF-STEM) image of a 15-HEA nanoparticle illustrates a crystalline structure with an FCC pattern, proving the material's single-phase structure at the nanoscale (Figure 2F). In addition to the particle-level elemental maps in Figure 1D, we show a low-magnification mapping of the 15-HEA sample, in which all the elements are homogeneously mixed in the nanoparticles (Figure 2G). We also confirmed the homogeneous mixing of these elements by using a Ni based TEM grid (Figure S4).

The uniform alloying among these strongly repelling combinations (e.g., Au-Mo, Au-W) showcases the power of using the increased entropic design ($T\Delta S_{\text{mix}}$) to overcome the immiscibility and achieve extreme mixing. Although our synthesis is conducted in Au-based combinations, this proof of concept demonstrates the feasibility of extending the enthalpy limit of alloying by a high-temperature and high-entropy strategy, which should be generally applicable to other systems as well.

Entropic contribution to induce metal reduction and stabilization

Another critical issue for nanoscale alloying is a tendency toward oxidation. For high-temperature metal reduction, an Ellingham diagram^{33,34} (Figure 3A), which illustrates the oxidation potential ($\Delta G_{\text{oxidation}}$) of different elements and the relative ease of reducing an oxide, is often used in metallurgy. Typically, elements on the top have a smaller oxidation potential and their oxides can be reduced by the metallic elements below them. In particular, carbon is ubiquitously used as a high-temperature reducing reagent through the carbothermal reduction ($x\text{C} + \text{MO}_x \xrightarrow{\text{high } T} \text{M} + x\text{CO}\uparrow$) for elements above the carbon oxidation line (i.e., green line in Figure 3A).^{33–36} Note that the Ellingham diagram is summarized for bulk materials with 1 atm O_2 partial pressure, which largely deviates from our nanoscale materials and synthesis in an inert Ar atmosphere. Therefore, the Ellingham diagram only acts as a guideline for the relative oxide potentials of different elements.

In our synthesis, as carbon substrates are employed for Joule heating and high-temperature synthesis, they also serve as natural reducing agents for elements above the carbon oxidation line. To verify the nanoscale carbothermal reduction (CTR), we synthesized Mo nanoparticles under three different conditions: (1) high-temperature CTR (1800 K, 50 ms); (2) low-temperature CTR (800 K, 50 ms three times); and (3) high-temperature heating on an oxide substrate (SiO_2 , 1,800 K, 1 s). The X-ray photoelectron spectroscopy (XPS) profiles (Figure 3B) clearly show that Mo is metallic under high-temperature CTR, while low-temperature synthesis or a lack of carbon could lead to a mixture of metallic and oxidized Mo states. We also verified the high-temperature CTR in Co, W, and Hf, where Co and W (above carbon) can be successfully made into metallic nanoparticles, while Hf remains oxidized (Figure 3C). As illustrated in Figure 3D, at nanoscale, noble elements (e.g., Pt) are easily reducible at high temperature; transition elements above carbon can be reduced by our high-temperature CTR method (e.g., Co, W, Mo), while those deep oxides below carbon will remain in oxidized states (e.g., Hf, Zr) due to their high oxidation potentials (Figure S5).

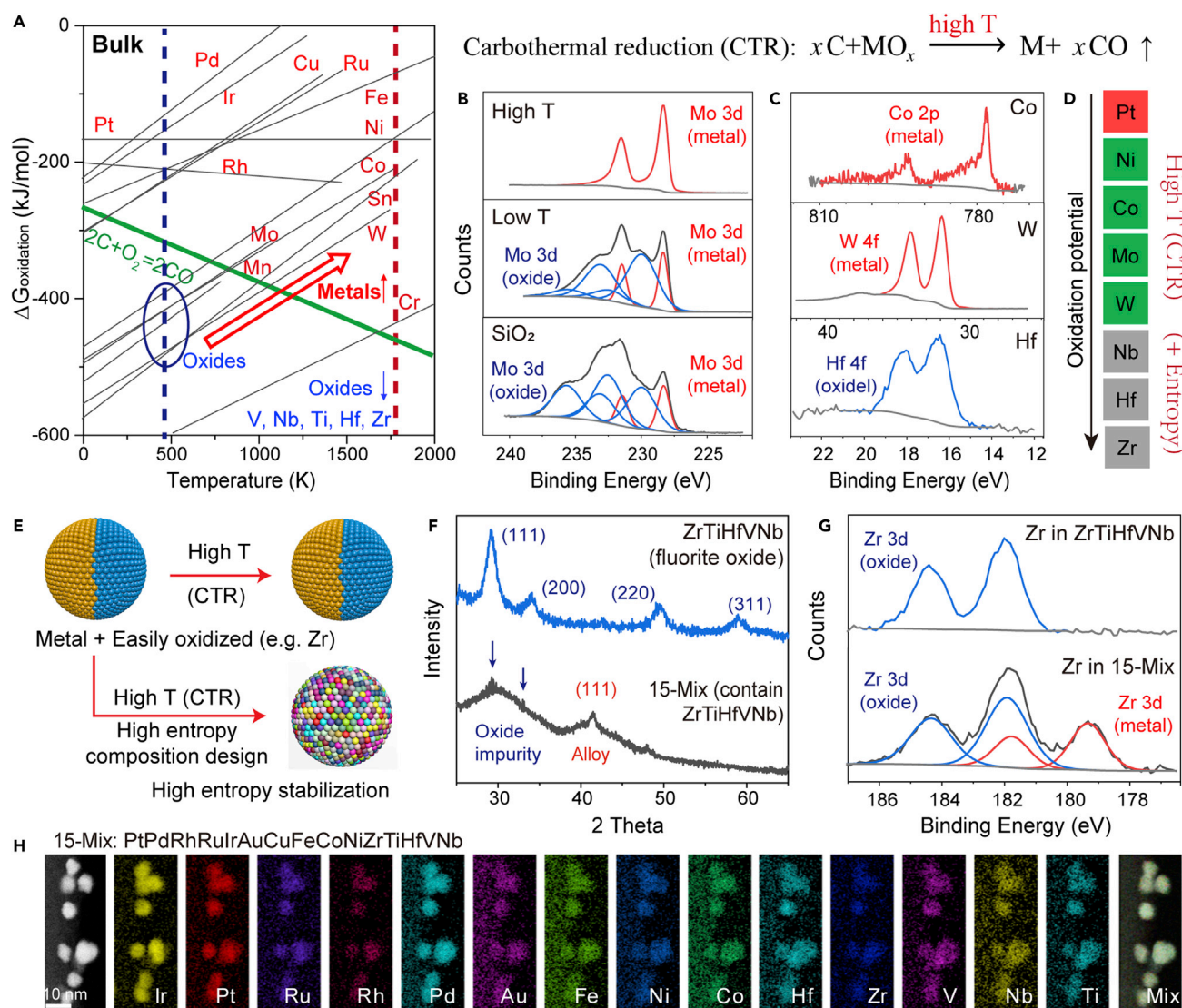


Figure 3. High-temperature- and high-entropy-induced metal reduction

(A) Ellingham diagram^{37,38} showing the elemental oxidation potentials and relative ease of metal reduction (bulk materials, 1 atm partial pressure O_2). The elements above the carbon oxidation line ($2C + O_2 \rightarrow 2CO \uparrow$) can be reduced by CTR synthesis.

(B) XPS profiles of Mo nanoparticles synthesized (in Ar atmosphere) by high-temperature CTR (High T), low-temperature CTR (Low T), and high-temperature heating on an oxide substrate (SiO_2). High-temperature CTR is the only method to achieve metallic Mo at the nanoscale.

(C) XPS profiles of Co, W, and Hf synthesized by high-temperature CTR, where Co and W are metallic while Hf is oxidized.

(D) List of nanoscale transition metal reduction by high-temperature CTR synthesis.

(E) Illustration of easily oxidized element stabilized by combining with a high-entropy compositional design.

(F) XRD profiles of ZrTiHfVNb (single-phase fluorite oxide) and 15-Mix (a mixture of metallic FCC with oxide residue).

(G) XPS profiles of Zr in ZrTiHfVNb (completely oxidized) and Zr in 15-Mix (metallic Zr and oxidized Zr). Specifically, the higher entropy converts part of Zr and stabilizes it into a metallic alloy.

(H) STEM elemental maps of 15-Mix, showing incorporation of ZrTiHfVNb elements in the metallic alloy nanoparticles (Cu not mapped). See also Figures S5–S7.

For those deep oxides, considering that high entropy strongly favors alloy mixing, we hypothesize that by combining high-temperature CTR and high-entropy design, the unique high-entropy structure could thermodynamically and kinetically stabilize these deep oxide elements into the metallic alloys (Figure 3E). We therefore increased the system entropy to a 15-element system to form PtPdRhRuIrAuCuFeCoNiZrTiHfVNb

(denoted 15-Mix). The XRD profile of 15-Mix shows a weak metallic FCC structure with some oxide impurity peaks, and these impurity peaks are similar to a fluorite structure formed by $(\text{ZrTiHfVNb})\text{O}_x$ (Figure 3F). The XPS result clearly reveals a mixture of metallic Zr and oxidized Zr in the 15-Mix sample, illustrating that a part of element Zr can be successfully incorporated into the 15-Mix system as metallic state (Figure 3G). This contrasts with the Zr element in ZrTiHfVNb where Zr is completely oxidized (Figure 3G) and verifies our hypothesis that a high-entropy structure could easily stabilize the oxide elements into metallic alloys thermodynamically and kinetically. We also confirmed the metal reduction effect of elements Hf and Nb in the 15-Mix sample as compared with them being complete oxides in a low-entropy configuration (Figure S6). STEM EDS maps further illustrate the elemental distribution in 15-Mix, where ZrTiHfVNb elements were found partially incorporated in the metallic alloy (Figure 3H). At a larger scale, we also revealed the mixture structure of metallic alloy and oxide impurities in 15-Mix (Figure S7). Therefore, while high temperature can induce carbothermic reduction to avoid oxidation, the high-entropy design is critical in stabilizing these elements by kinetically or physically confining them inside the alloy structure away from oxidation.

Detailed characterization of entropy-stabilized nanoalloys

All of the above alloys are achieved by overcoming immiscibility and inducing metal reduction, leading to extreme mixing with unique entropy-stabilized nanostructures. Macroscopically, synchrotron XRD ($\lambda = 0.2113 \text{ \AA}$) was used to characterize the 15-HEA nanoparticles because it provides better structural resolution than conventional XRD. As shown in Figure 4A, the majority of the diffraction peaks can be indexed using an FCC packing with a unit cell size of $3.78 \text{ \AA}$. The single-phase FCC packing is mostly a composition effect, as most elements in the 15 HEA nanoparticles favor FCC structure in their individual metals. Other structures, such body-centered-cubic, could be achieved if those refractory elements could be alloyed into HEA nanoparticles.³⁹ Compared with the typical synchrotron profile of simple metals,⁴⁰ the diffraction peaks overall are broader, particularly for high-angle peaks, which may be due to the small particle size and the extremely disordered structure among the 15 largely different elements.

We also examined the bonding structures of the 15-HEA nanoparticles using X-ray absorption spectroscopy (XAS) for elements (PdRhRuIrCuFeNiWMoCrMnSn) and their respective metal foils as reference (Figures S8 and S9). Notably, the Fourier-transformed extended X-ray absorption fine structures (FT-EXAFS) profiles representing Ir, Ru, Fe, and W—from the 3d, 4d, and 5d elements in the 15-HEA alloy—all show a similar metallic bonding distance around $2 \text{ \AA}$ with slight variations in peak position, confirming a uniform alloy bonding with local fluctuations or short-range ordering^{26,41,42} (Figure 4B). This contrasts with their corresponding metal foils showing drastically different bonding configurations. The similarity in the metal bonding for different elements in the 15-HEA alloys illustrates the homogeneous distribution of metal elements and a uniform alloy structure without obvious metal segregations. The synchrotron XRD and XAS results, therefore, confirm an alloy structure and uniform bonding environment in 15-HEA nanoparticles at a macroscopic scale with high resolution.

Microscopically, we used a state-of-the-art four-dimensional (4D)-STEM technique^{43–46} to observe the detailed structure and local strain behavior in the 15-HEA nanoparticles. In 4D-STEM, an electron probe is rastered across a selected region of interest (two-dimensional [2D] real space), and at each probe position a diffraction pattern is acquired (2D reciprocal space). From these diffraction patterns, local structural information, such as strain and lattice distortions, is

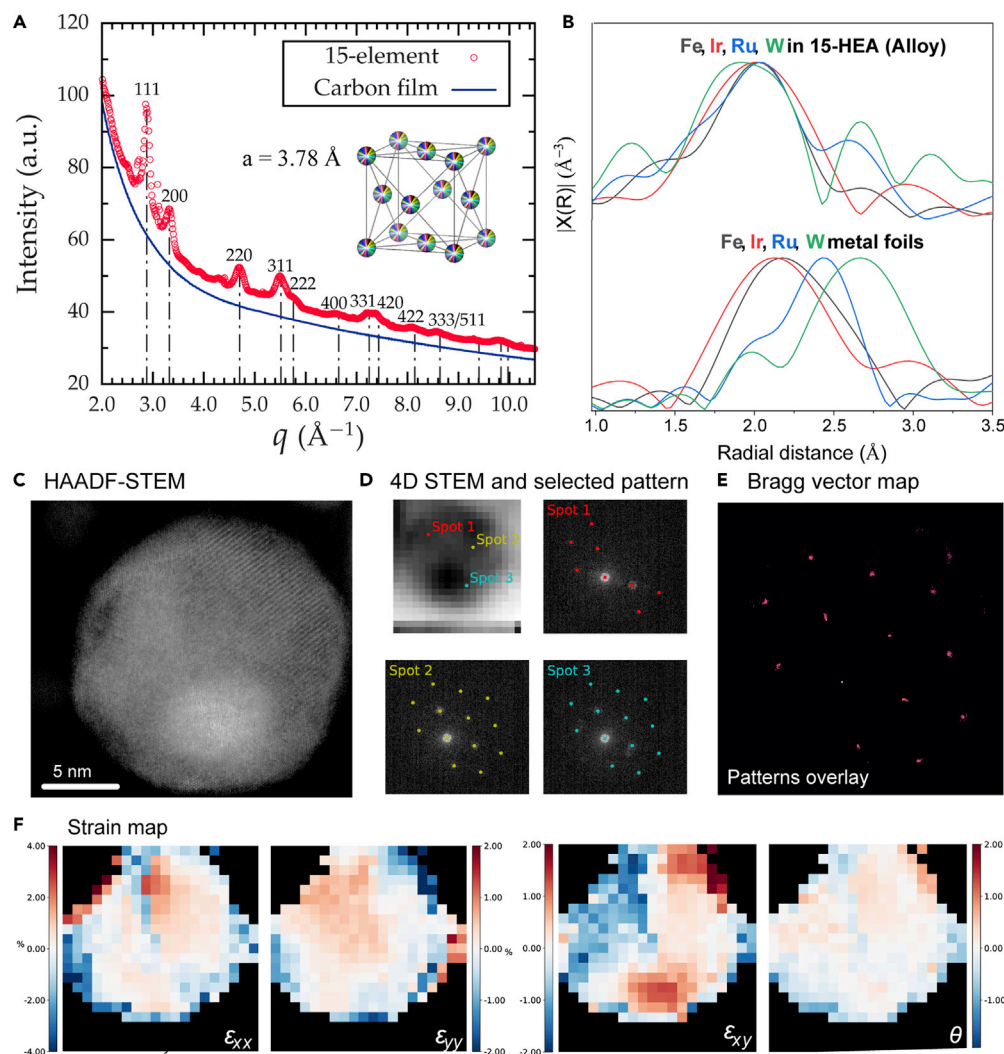


Figure 4. Detailed structural study of the 15-HEA nanoparticles

(A) Macroscopic synchrotron XRD of the 15-HEA nanoparticles, showing an overall single-phase FCC structure.

(B) FT-EXAFS profiles of Fe, Ir, Ru, and W measured in the 15-HEA nanoparticles and comparison with their corresponding pure metal foils, suggesting alloy formation due to the variation in peak position.

(C) High-magnification HAADF-STEM image of a 15-HEA nanoparticle, on which a 4D-STEM dataset of this particle was acquired.

(D) Subsequently generated virtual ADF image in which each pixel corresponds to a diffraction pattern. Three selected diffraction patterns at various locations within this particle are shown.

(E) Bragg vector map showing overlay of all diffraction patterns within the particle.

(F) Strain map of the 15-HEA nanoparticle calculated from the variation in the lattice, showing the localized strain and inhomogeneity in the nanoparticle due to extreme mixing.

See also Figures S8–S11.

determined. Figure 4C shows an atomically resolved HAADF-STEM image of a singular 15-HEA nanoparticle, and a 4D-STEM dataset of this particle was acquired. As demonstrated in Figure 4D, each pixel of the virtual annular dark-field (ADF) image corresponds to a diffraction pattern. Three selected diffraction patterns at different locations within the particle are shown, from which the local structure (lattice constant and strain deformation) are derived. The resulting Bragg vector map (an average deconvolution of all acquired diffraction patterns) indicates the nanoparticle is single crystalline with FCC structure at the single-particle level (Figure 4E).

Localized strain information was calculated using this map as well as the individual diffraction patterns acquired at each point (Figure 4F). The strain maps are calculated according to the variation within individual diffraction patterns as they compare with the average Bragg vector map. Thus, 0% strain change indicates that these regions are comparable with the average Bragg vector map. The step size used is 1 nm/pixel, therefore significant shifts in strain (from tensile to compression) are confined to approximately one to two pixels within the particle (~1–2 nm). As an aside, the bright contrast within the HAADF-STEM image of the nanoparticle is assumed to be a secondary particle, owing to the secondary diffraction pattern observed in Spot 3. It appears to us that the second particle does not disrupt the lattice columns of the primary particle and does not have diffraction patterns indicative of a grain boundary. We therefore assume it is an attachment rather than being inside the primary particle. This secondary particle was excluded from the overall strain map by determining the secondary diffraction pattern and creating a mask for these disks.

The generated strain map of this singular nanoparticle demonstrates strain inhomogeneity, as both tensile (red) and compression (blue) strain are observed. From EDS data of this same region (Figure S10), there does not appear to be chemical inhomogeneity. The changes in strain do correlate with changes in the atomic lattice observed in the atomic-resolution HAADF-STEM image (Figure 4C). We observe that the majority of the strain inhomogeneity, a sharp pixel-to-pixel change from compression to tension or low strain to high strain, is confined to the edges of the particle as well as the boundaries between the changes in atomic lattice fringes. Excluding these rapid changes, the variation of strain within the particle is less than $\pm 0.5\%$, which is likely related to short-range ordering and distortions due to the extreme mixing of 15 elements with differing crystal structures. This observation indicates that although HEA nanoparticles overall are in a single-phase structure, they are not completely random or uniform; rather, there are natural composition and structure fluctuations (e.g., short-range ordering) leading to local heterogeneity within the materials and causing localized strain and lattice distortions.^{41,44,47}

Despite these localized strains and distortions, we confirmed that 15-HEA nanoparticles are thermally stable by *in situ* heating in the TEM chamber up to 600°C (Figure S11). Both the size distribution and alloy structure exhibited no obvious change during the *in situ* heating process (isothermal holding for at least 30 min). The thermal and structural stability may come from the entropy stabilization effect, whereby a high-entropy structure is stabilized both thermodynamically ($\Delta G_{\text{mix}} = \Delta H_{\text{mix}} - T\Delta S_{\text{mix}}$) and kinetically (sluggish diffusion due to large distortions).^{16,28,30,42} The 4D-STEM result in particular clearly illustrated strain and distortions in the lattice of entropy-stabilized 15-HEA nanoparticles, which could serve as local diffusion barriers for phase separation and therefore improve the structural stability. Additionally the strain inside the nanoparticles could largely tune the performance, especially for catalysis.^{26,48}

DISCUSSION

To summarize our synthesis strategy, we plotted the transition metal alloying guided by the mixing enthalpy and oxidation potentials as a reference (Figure 5A). Conventionally, easily mixed alloys are found under restrictive conditions with a mild mixing enthalpy (e.g., $\Delta H_{\text{mix}} < 3.57$ kJ/mol) and easily reducible elements (e.g., $\Delta G_{\text{oxidation}} > -300$ kJ/mol). To extend the alloy spaces, we used extreme entropic contribution ($-T\Delta S_{\text{mix}}$) to drive alloy formation, for example,

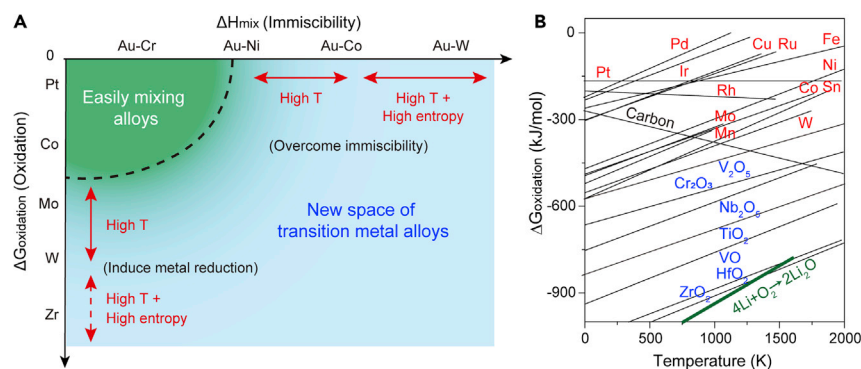


Figure 5. Strategies for extending the metallic alloying spaces at the nanoscale

(A) Extended alloy space of transition metals at the nanoscale by overcoming immiscibility and inducing metal reduction. In these processes, high temperature and high entropy are critical to driving the alloy formation in a large range of immiscibility (x axis) and oxidation potentials (y axis). The solid arrow indicates metallic alloys formed in the range, while the dashed arrow indicates partial metal reduction and stabilization.

(B) Ellingham diagram with more easily oxidized elements included. Notably, lithium is at the lowest position and can reduce the elements above the lithiothermic reduction line to achieve metallic alloys with these easily oxidized elements.

See also [Figure S12](#) and [Note S1](#).

high-temperature 1,800 K synthesis combined with a 15-element high-entropy design. As demonstrated, the limiting enthalpy was elevated to Au-Co (~ 10 kJ/mol) by high-temperature synthesis and further to Au-W (~ 25 kJ/mol) by combining with high-entropy-driven mixing, which could cover all the possible binary combinations in the transition metal space.¹⁰ Additionally, using the Ellingham diagram as a guide, our high-temperature synthesis induced carbothermal reduction to convert transition elements (e.g. Ni, Mo, W) into metallic nanoparticles, including some partial refractory metals (e.g., Zr), by high-entropy compositional design. Therefore, our entropically driven synthesis largely extends the alloy spectrum in transition metals by overcoming the immiscibility and inducing metal reduction, enabling a vast space for alloy exploration that is full of potential for broad applications.

In addition, it is noteworthy that there are still deep oxide transition metals (mostly refractory metals) that have not been made into nanoscale alloys. Inspired by nanoscale carbothermal reduction, we propose that these easily oxidized elements can be reduced to the metallic alloy by nanoscale metallothermic reduction.^{35,36,49,50} As illustrated in [Figure 5B](#), lithium has the lowest oxidation potential and therefore highest reduction capability through the lithiothermic reduction reaction ($2x\text{Li} + \text{MO}_x \xrightarrow{\text{high } T} \text{M} + x\text{Li}_2\text{O}$).⁵¹ We presented some preliminary data on the lithiothermic reduction of refractory metals at the nanoscale, showing XRD and electrochemical tests suggesting potential metal reduction ([Figure S12](#) and [Note S1](#)); however, the metals are easily oxidized when exposed again in the air. Further reduction and stabilization strategies would be a promising direction to take to extend alloying toward those easily oxidized elements at the nanoscale.

Lastly, in this paper the extreme mixing in our 15-element nanoalloy highlights the capability of alloying strongly immiscible combinations and easily oxidized elements. Compared with the number of mixes, the types of the constituent elements are more important in gaining qualification as an extreme mixing alloy. In our design, high entropy benefits alloy formation thermodynamically and kinetically. From a

thermodynamic point of view, high entropy naturally favors a random mixing structure (i.e., alloy formation) based on the Gibbs free energy consideration ($\Delta G_{\text{mix}} = \Delta H_{\text{mix}} - T\Delta S_{\text{mix}}$), whereby the increase in the entropy (also the temperature) will largely decrease the mixing Gibbs free energy and therefore drive alloy formation. From a kinetic point of view, high-entropy structure features a random mixing of many different elements, which can cause large lattice distortions and strain inhomogeneity inside the particle. The distorted structures can also “trap” or “freeze” the mixing structure inherited from the high-temperature synthesis due to difficulties in atom diffusion and structure relaxation. It should be noted that besides entropy considerations, other physicochemical properties will also affect the single-phase mixing, for example, atom size mismatch, valence electron concentration, and the size effect.⁵² Therefore, the entropy-driven strategy acts as an important methodology and descriptor for alloy mixing, yet the precise evaluation of each contributing parameter will require more experiments and perhaps a data-driven discovery process.^{15,17}

Conclusion

In this paper, we explored an entropic design strategy ($-T\Delta S_{\text{mix}}$) for single-phase alloy formation at the nanoscale among transition metal elements—specifically, how different elements can be successfully incorporated into an alloy structure and what the potential alloying capabilities are. By systematic synthesis and exploration of many alloy nanoparticles, we found that the mixing enthalpy (implication of immiscibility) and Ellingham diagram (implication of oxidation potential) are critical guidelines for structure prediction. By following the alloying guidelines, we have used the high-temperature and high-entropy design to achieve record-high 15-element HEA nanoparticles by overcoming immiscibility in strongly repelling combinations and inducing metal reduction for easily oxidized elements. These unique alloy nanoparticles demonstrate overall uniform mixing with localized strain and distortions, which may be a unique characteristic of the extreme mixing of so many dissimilar elements. Our synthesis largely expands the spectrum of possible transition metal alloys and enables a range of previously inaccessible elemental combinations and alloy structures. This vast compositional space is also intriguing for future data-driven material discovery and broad technological applications.

EXPERIMENTAL PROCEDURES

Resource availability

Lead contact

Further information and requests for resources and materials should be directed to and will be fulfilled by the lead contact, Liangbing Hu (binghu@umd.com).

Materials availability

All materials generated in this study will be made available on reasonable request.

Data and code availability

The acquired datasets were analyzed using py4DSTEM, an open-source Python program available on Github (<https://github.com/py4dstem/py4DSTEM>).

High-temperature shock process

The high-temperature shock synthesis was performed through Joule heating of precursor-loaded carbon nanofiber films in an argon-filled glovebox, similar to the method reported previously.⁵ On brief, individual metal salts or their hydrate forms (Sigma-Aldrich) were dissolved in ethanol at a concentration of 0.05 mol/L. The alloy precursors were mixed in the solution phase at a 1:1 molar ratio and loaded

onto a carbon nanofiber film using a pipette with a loading of $5 \mu\text{mol}/\text{cm}^2$. The high-temperature synthesis was triggered by electric Joule heating using a Keithley 2425 SourceMeter. The shock temperature and duration was tuned by the input electrical power, which we monitored in-line with a home-made high-speed video system.⁵³

Structural characterization

The microstructure was characterized by a scanning electron microscope (Hitachi SU-70 FEG-SEM at 10 kV) and transmission electron microscopes (JEOL 2100F FEG TEM/STEM operated at 200 kV, and JEOL TEM/STEM ARM 200CF). The elemental distribution and maps were measured using an Oxford X-max 100TLE windowless X-ray detector. XRD was performed using a D8 Advanced (Bruker AXS, WI, USA) with a scan rate of $3^\circ/\text{min}$. XPS was performed on Kratos Axis 165 spectrometer. Synchrotron XRD experiments were carried out at the 11-ID-B beam-line of the Advanced Photon Source at Argonne National Laboratory (Chicago, IL, USA). The X-ray wavelength was $0.2113 \text{ \AA}$, and the sample-to-detector distance was 175.1 mm. Reduction of 2D diffraction patterns to 1D profiles, as well as diffraction peak indexing and Rietveld refinement, were performed using GSAS-II software.

X-ray absorption spectroscopy measurement and analysis

XAS data were collected from the CLS@APS (Sector 20-BM) beamline at the Advanced Photon Source (operating at 7.0 GeV) at Argonne National Laboratory. The sample was measured in fluorescence mode simultaneously with a reference for each element at room temperature and ambient pressure, protected from exposure with oxygen using a sealed aluminum pouch. EXAFS data were normalized and transformed into k-space and R-space using the Athena program with conventional procedures. The k-range used to generate the FT-EXAFS spectra for each element was as follows: $3.0\text{--}9.3 \text{ \AA}^{-1}$ for Cr, $2.3\text{--}11.8 \text{ \AA}^{-1}$ for Cu, $2.2\text{--}10.0 \text{ \AA}^{-1}$ for Fe, $2.5\text{--}9.3 \text{ \AA}^{-1}$ for Ir, $2.4\text{--}8.9 \text{ \AA}^{-1}$ for Mn, $2.2\text{--}11.9 \text{ \AA}^{-1}$ for Mo, $2.2\text{--}10.3 \text{ \AA}^{-1}$ for Ni, $2.3\text{--}11.9 \text{ \AA}^{-1}$ for Pd, $2.0\text{--}11.8 \text{ \AA}^{-1}$ for Rh, $2.1\text{--}11.7 \text{ \AA}^{-1}$ for Ru, $2.9\text{--}11.7 \text{ \AA}^{-1}$ for Sn, and $3.1\text{--}12.0 \text{ \AA}^{-1}$ for W. A k-weighting of 2 was used for each element except for Mn, which used a k-weighting of 1.

Fast scanning electron microscopy

4D-STEM datasets were acquired with a Gatan Orius 830 CCD using an FEI TitanX operated at 300 kV with a beam size of 2 nm and a probe semi-convergence angle of 0.48 mrad. The acquired datasets were subsequently analyzed using py4DSTEM, an open-source Python program available on Github (<https://github.com/py4dstem/py4DSTEM>).

SUPPLEMENTAL INFORMATION

Supplemental information can be found online at <https://doi.org/10.1016/j.matt.2021.04.014>.

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AUTHOR CONTRIBUTIONS

Conceptualization, L.H. and Y.Y.; Methodology, Y.Y., J.G., T.L., Q.D., and M.J.; Investigation, Y.Y., Z.H., R.S.-Y., L.A.H., S.E.Z., B.H.S., C.O., A.M.M., D.M., Z.F., P.Z., M.C., Y.M., and J.L.; Writing – original draft, L.H. and Y.Y.; Writing – review & editing, all authors; Supervision, L.H.

DECLARATION OF INTERESTS

L.H. is a co-founder of HighT-Tech and a member of its scientific advisory board. All research reported in this paper was performed at the University of Maryland or by collaborators and is the intellectual property of the University of Maryland, not HighT-Tech. HighT-Tech has an exclusive license from the University of Maryland for the commercialization of this type of technology.

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